## MathMatrix

IEC 61131 Library for AcSELERATOR RTAC ${ }^{\circledR}$ Projects

## SEL Automation Controllers

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## RTAC LIBRARY

## MathMatrix

## Introduction

The MathMatrix library allows for the creation of matrices of complex numbers. There are multiple desired workflows that exist when working with matrices and the library provides several options for working with them.
The library is designed to facilitate two basic types of matrix operations: operations that modify an existing matrix and operations that take one or more matrices as arguments and place the result in a different matrix. Operations that affect only the active matrix are completed using the methods on class_Matrix objects. Operations that affect two or more matrices are performed by external functions or special matrix manipulation classes.

The library also allows for operations of varying levels of required immediacy. For work on large or highly variant sized matrices that can be completed over multiple task cycles, it provides matrix manipulation classes that are loaded with operator and result matrices, stimulated to run to completion, and given a fixed number of steps or a fixed time slice. For operations that must complete immediately, ideally on fixed sized matrices so the computation time can be evaluated to validate timing requirements, functions provided by the library accomplish the same work while guaranteeing the completion of the algorithm before returning.
This library is dependent on the capabilities defined in the MathComplex library for all operations (see the MathComplex library documentation for more information on the operation of this library).

## Special Considerations

- Copying classes from this library causes unwanted behavior. This means the following:

1. The assignment operator " $:=$ " must not be used on any class from this library; consider assigning pointers to the objects instead.
```
// This is bad and in most cases will provide a compiler error
    such as:
// "C0328: Assignment not allowed for type
    class_MathMatrixObject"
myMathMatrixObject := otherMathMatrixObject;
```

NOTE: Because of the cost of checking the system time, the time is not validated at each step in the algorithm but rather after multiple steps have been completed.

```
// This is fine
someVariable := myMathMatrixObject.value;
// As is this
pt_myMathMatrixObject := ADR(myMathMatrixObject);
```

2. Classes from this library must never be VAR_INPUT or VAR_OUTPUT members in function blocks, functions, or methods. Place them in the VAR_IN_OUT section or use pointers instead.

Classes in this library have memory allocated inside them. As such, they should only be created in environments of permanent scope (e.g., Programs, Global Variable Lists, or VAR_STAT sections).

Though this library provides the capability to dynamically resize, create, and destroy matrices, memory operations can be long running and care should be taken to avoid unnecessary use of this type of operation on a time-critical task.

## Supported Firmware Versions

You can use this library on any device configured using ACSELERATOR RTAC ${ }^{\circledR}$ SEL-5033 Software with firmware version R143 or higher.

Versions 3.5.0.1 and older can be used on RTAC firmware version R132 and higher.

## Enumerations

Enumerations make code more readable by allowing a specific number to have a readable textual equivalent.

## enum_MatrixState

| Enumeration | Description |
| :--- | :--- |
| NOT_INITIALIZED | This matrix has no memory assigned to it, call SetSize() to <br> initialize. |
| NO_OPERATION | The matrix is not locked to any operation. |
| MATRIX_SCALE | The matrix is being scaled by one value. |
| EXTERNAL_OPERATION | The matrix is being operated on by an external class. |
| MATRIX_ROW_STEP_MULT | The matrix is multiplying a row by a scalar. |
| MATRIX_ROW_STEP_DIV | The matrix is dividing a row by a scalar. |
| MATRIX_ROW_STEP_ADD | The matrix is adding two rows together. |
| MATRIX_ROW_STEP_SUB | The matrix is subtracting one row from another. |

## Functions

## fun_DeleteMatrix (Function)

The user should call this after completing work on a matrix received through fun_NewMatrix () before the matrix goes out of scope. It releases all system resources.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| pt_matrix | POINTER TO class_Matrix | The matrix to be deleted. This pointer must be re- <br> ceived through fun_NewMatrix. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | TRUE if the memory is successfully deallocated. |

## Processing

This function frees all system resources owned by this matrix. After completion of the function, pt_matrix is NULL(0).

## fun_MatrixAdd (Function)

This function adds two matrices and places the result in a third. The entire operation will complete before the function returns.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| matrix1 | class_Matrix | The first addend. |
| matrix2 | class_Matrix | The second addend. |
| result | class_Matrix | The sum of the two matrices. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | The matrix addition completed successfully. |

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## Processing

This function sets the return value to TRUE if all conditions for performing the addition are met as follows:

- matrixl and matrix2 are initialized.
- All three matrices are not busy performing a stepwise operation.
- result is a separate matrix from both matrixl and matrix2.
- matrixl and matrix2 have the same dimensions.
- If necessary, result is successfully resized.

It then performs the addition.

## fun_MatrixCopyColumn (Function)

This function copies one column from one matrix to a column in a second matrix. The entire operation will complete before the function returns.

## Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| fromColumn | UINT | The column index of the column being copied from. |
| toColumn | UINT | The column index of the column being copied to. |

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| fromMatrix | class_Matrix | The matrix being copied from. |
| toMatrix | class_Matrix | The matrix being copied to. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | The column copy completed successfully. |

## Processing

This function sets the return value to TRUE if all conditions for performing the copy are met as follows:

Both matrices are initialized.

- Both matrices are not busy performing a stepwise operation.
- Both matrices have the same number of rows.
- The column indices provided are within the size of the matrices referenced.

It then performs the copy.

## fun_MatrixDeterminant (Function)

This function calculates the determinant of a square matrix. The entire operation will complete before the function returns.
If the purpose behind calculating the determinant is a check before inverting a matrix or as part of the process of solving a system of equations this class is not the most optimal to use. In these cases it is better to use the fun_MatrixInvert or the fun_MatrixGaussianElim object instead as the overhead for all three is similar.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| original | class_Matrix | The matrix to calculate the determinant of. This matrix is <br> left unchanged. |
| workspace | class_Matrix | Memory to do the calculation in. If this is the same size <br> as original, no memory allocation will occur in finding the <br> determinant. |

Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| determinant | struct_ComplexRect | The determinant of the matrix. Zero if the matrix is not <br> invertible. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the operation was attempted. |

## Processing

1. This function sets the return value to TRUE if all conditions for performing the calculation are met as follows:
> original is initialized.
> original is a square matrix.

- workspace is a separate matrix from original.
> Neither matrix is busy performing some other operation.
- If necessary, workspace is successfully resized.

2. Copies the contents of original into workspace.
3. Reduces workspace to an identity matrix using elementary row operations.
4. Calculates the determinant from the row operations performed.
5. If at any time the row operations cannot reduce workspace further and it is still not an identity matrix, the operation is terminated and determinant is set to zero.

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## fun_MatrixGaussianElim (Function)

This function simplifies a matrix to a diagonal ones matrix with trailing columns using Gaussian elimination. The contents of coefficients are destroyed and the contents of solutions are modified by this function. The entire operation will complete before the function returns.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| coefficients | class_Matrix | The coefficients of the variables being solved for. |
| solutions | class_Matrix | The right hand side of the system of equations. |

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| error | BOOL | This algorithm cannot solve this system of equations. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the Gaussian elimination was attempted and the matrices <br> could have been modified. |

## Processing

This function sets the return value to TRUE if all conditions for performing the calculation are met as follows:
$>$ Both matrices are initialized.
> Both matrices are not busy performing a stepwise operation.
$>$ coefficients is a separate matrix from solutions.
$>$ coefficients has at least as many columns as rows.
$>$ solutions has the same number of rows as coefficients.
Reduces the first Rows • Rows of coefficients to an identity matrix using elementary row operations.

Performs the same row operations on solutions.
> If at any time the row operations cannot reduce coefficients further and there is still not an identity matrix on the left the operation is terminated and error is set.

- The contents of coefficients are destroyed and the contents of solutions are modified by this method.


## Output Combination Meanings

| Error | Return | Description |
| :--- | :--- | :--- |
| FALSE | FALSE | This should never occur. |
| FALSE | TRUE | The Gaussian elimination completed successfully. |
| TRUE | FALSE | The matrix state prevented the Gaussian elimination request. |
| TRUE | TRUE | The matrix is not invertible and cannot be reduced by this Gaussian elimi- <br> nation algorithm. |

## fun_MatrixInvert (Function)

This function creates the inverse of a square matrix. original is destroyed in the process so if the data are still desired, they must be copied before the function is called. The entire operation will complete before the function returns.

One common use case for inverting a matrix is to solve a system of equations. In this library that use case is discouraged unless solving the same system for many solutions as Gaussian elimination performs the same functionality with less overhead.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| original | class_Matrix | The matrix to invert. |
| result | class_Matrix | The inverted matrix. |

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| error | BOOL | The inversion could not be attempted or original cannot be in- <br> verted. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if inversion was attempted and the matrices could have been <br> modified. |

## Processing

1. This function sets the return value to TRUE if all conditions for performing the calculation are met as follows:
> original is initialized.

- Both matrices are not busy performing a stepwise operation.
- result is a separate matrix from original.
> original is a square matrix.
- If necessary, result is successfully resized.

2. Sets result to an identity matrix.
3. Reduces original to an identity matrix using elementary row operations.
4. Performs the same row operations on result to create the inverse.
5. If at any time the row operations cannot reduce original further and it is still not an identity matrix, the operation is terminated and error is set.

## Output Combination Meanings

| Error | Return | Description |
| :--- | :--- | :--- |
| FALSE | FALSE | This should never occur. |
| FALSE | TRUE | The inversion completed successfully. |
| TRUE | FALSE | The matrix state prevented the inversion request. |
| TRUE | TRUE | The matrix is not invertible. |

## fun_MatrixMultiply (Function)

This function multiplies two matrices and places the result in a third. The entire operation will complete before the function returns.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| matrix1 | class_Matrix | The multiplier. |
| matrix2 | class_Matrix | The multiplicand. |
| result | class_Matrix | The product of the two matrices. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | The matrix multiplication completed successfully. |

## Processing

This function sets the return value to TRUE if all conditions for performing the calculation are met as follows:

- matrix1 and matrix2 are initialized.
- All three matrices are not busy performing a stepwise operation.
- result is a separate matrix from both matrixl and matrix2.
> The column count of matrixl equals the row count of matrix2.
If necessary, it sets the size of result. It then performs the multiplication.


## fun_MatrixSubtract (Function)

This function subtracts one matrix from another and places the result in a third. The entire operation will complete before the function returns.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| matrix1 | class_Matrix | The minuend. |
| matrix2 | class_Matrix | The subtrahend. |
| result | class_Matrix | The difference of the two matrices. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | The matrix subtraction completed successfully. |

## Processing

This function verifies that the subtraction can be performed:

1. matrixl and matrix2 are initialized.
2. All three matrices are not busy performing a stepwise operation.
3. result is a separate matrix from both matrixl and matrix2.
4. matrixl and matrix2 have the same dimensions.

If necessary, the function resizes result. It then performs the subtraction.

## fun_MatrixTranspose (Function)

This function places the transpose of a matrix into a result. The entire operation will complete before the function returns.

## Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| conjugate | BOOL | The result of this operation will be the Hermitian Transpose. <br> Before each element is placed in result, it will be conjugated. |

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| original | class_Matrix | The matrix whose transpose is calculated. |
| result | class_Matrix | The transpose of the original matrix. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | The matrix transpose completed successfully. |

## Processing

This function verifies that the transpose can be performed:

1. original is initialized.
2. Both matrices are not busy performing a stepwise operation.
3. result is a separate matrix from original.

If necessary the function resizes result. It then performs the transpose. If conjugate is TRUE, conjugate each element in result.

## fun_Matrix_ATA (Function)

This function performs an optimization of the operation $\left(\mathrm{A}^{\mathrm{T}} \mathrm{A}\right)$ transposing an input matrix and multiplying it by itself. The entire operation will complete before the function returns.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| conjugate | BOOL | The result of this operation will be calculated using the Her- <br> mitian Transpose. Before the transpose step is complete, each <br> element will be conjugated. |

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| original | class_Matrix | The matrix A. |
| result | class_Matrix | The matrix for the result. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the operation completed successfully. |

## Processing

This function verifies that the operation can be performed:

1. original is initialized.
2. Both matrices are not busy performing a stepwise operation.
3. result is a separate matrix from original.

If necessary, the function resizes result. It then performs the operation $\mathrm{A}^{\mathrm{T}} \mathrm{A}$. If conjugate is TRUE, conjugate each element in the transpose before using it in the multiply.

## fun_NewMatrix (Function)

Request a new matrix from the system with all required resources. Matrices received through this function must be freed through the fun_DeleteMatrix() function before they leave scope.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| rows | UINT | The number of rows in the new matrix. |
| cols | UINT | The number of columns in the new matrix. |

Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| POINTER TO class_Matrix | The address of the new class_Matrix. |

## Processing

This function allocates system resources for a rows by cols matrix of struct_ComplexRect objects.

## Classes

This library provides the following classes as extensions of the IEC 61131 function block.

## class_Matrix (Class)

This is the fundamental class for this library. It allows for the storage of struct_ComplexRect objects ordered by row and column. It manages all required system resources internally.

## Initialization Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| rowCount | UINT | The number of rows this matrix begins with. |
| colCount | UINT | The number of columns this matrix begins with. |

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| pt_Data | POINTER TO POINTER TO <br> struct_ComplexRect | Pointer to an array of pointers (one for each <br> row). Allows accessing the matrix with [row][col] <br> syntax. Indexing starts at zero. This pointer should <br> be re-read before access after any resize operation. |
| Rows | UINT | The number of rows in the matrix. |
| Cols | UINT | The number of columns in the matrix. |
| State | enum_MatrixState | The active matrix operation. |

## Clear (Method)

This method returns all system resources internal to this matrix and sets its size to zero rows by zero columns. In addition it clears all locks on the matrix and resets all internal state machines.

This should typically be used only to free the system resources held by this matrix before it goes out of scope.

## MatrixRowAdd (Method)

This method adds one row to another inside this matrix, replacing the content of the second row (Matrix $[$ toRow $]=$ Matrix $[$ toRow $]+$ Matrix $[f r o m R o w] ~ \cdot s c a l a r)$. The entire operation will complete before the method returns.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| fromRow | UINT | The first addend. |
| toRow | UINT | The second addend and the location of the result. |
| scalar | struct_ComplexRect | A constant that is multiplied against the value of each entry <br> in fromRow before adding it to the entry in toRow. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method performed the addition. |

## Processing

1. Validates that the matrix is initialized and not in the middle of a stepwise operation.
2. Validates that the provided row indices exist.
3. If the checks pass, multiplies fromRow by scalar and adds the result to toRow.
4. fromRow remains unchanged.

## MatrixRowDivide (Method)

This method divides each element in rowIndex by scalar and stores the results back in rowIndex (Matrix $[$ rowIndex $]=$ Matrix $[$ rowIndex $] /$ scalar). The entire operation will complete before the method returns.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| rowIndex | UINT | The row to be modified. |
| scalar | struct_ComplexRect | A constant used as the divisor against the value of each entry <br> in rowIndex. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method performed the division. |

## Processing

1. Validates that the matrix is initialized and not in the middle of a stepwise operation.
2. Validates the row index provided exists.
3. If the checks pass, divides each entry in rowIndex by scalar.

## MatrixRowMultiply (Method)

This method multiplies each element in rowIndex by scalar and stores the results back in rowIndex (Matrix[rowIndex] = Matrix[rowIndex] • scalar). The entire operation will complete before the method returns.

## Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| rowIndex <br> scalar | UINT <br> struct_ComplexRect | The row to be modified. <br> A constant used as the multiplier against the value of each <br> entry in rowIndex. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method performed the multiplication. |

## Processing

1. Validates that the matrix is initialized and not in the middle of a stepwise operation.
2. Validates the row index provided exists.
3. If the checks pass, multiplies each entry in rowIndex by scalar.

## MatrixRowSubtract (Method)

This method subtracts one row from another inside this matrix, replacing the content of the second row (Matrix $[t o R o w]=$ Matrix $[t o R o w]-$ Matrix $[$ fromRow $]$ scalar). The entire operation will complete before the method returns.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| fromRow | UINT | The subtrahend. |
| toRow | UINT | The minuend and the location of the result. |
| scalar | struct_ComplexRect | A constant that is multiplied against the value of each entry <br> in fromRow before subtracting it from the entry in toRow. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method performed the subtraction. |

## Processing

1. Validates that the matrix is initialized and not in the middle of a stepwise operation.
2. Validates the row indices provided exist.
3. If the checks pass, multiplies fromRow by scalar and subtracts the result from toRow.
4. fromRow remains unchanged.

## MatrixScale (Method)

Multiplies each element in this matrix by a scalar. The entire operation will complete before the method returns.

## Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| scalar | struct_ComplexRect | A constant that is multiplied against the value of each entry this <br> matrix. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method scaled the matrix. |

## Processing

1. Validates that the matrix is initialized and not in the middle of a stepwise operation.
2. If the checks pass, multiplies each element in the matrix by scalar, placing the result in the same location.

## MatrixStepRowAdd (Method)

This method adds one row to another inside this matrix, replacing the content of the second row (Matrix $[$ toRow $]=$ Matrix $[t o R o w]+$ Matrix $[$ fromRow $]$ scalar $)$.

The operation will perform the next steps operations of the complete addition. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the addition. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise addition.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to multiply fromRow by scalar and add the result to toRow.
3. fromRow remains unchanged.
4. Performs, at most, the next steps operations toward completing the addition algorithm.
5. Decrements steps by the number of operations consumed.
6. Returns TRUE and unlocks the matrix if the addition completed.
7. Returns FALSE if the addition was not attempted or steps was exhausted before the algorithm completed.

## MatrixStepRowDivide (Method)

This method divides each element in toRow by scalar and stores the results back in toRow (Matrix $[$ toRow $]=$ Matrix $[t o R o w] /$ scalar $)$.

The operation will perform the next steps operations of the complete division. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the division. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise division.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to divide each element in toRow by scalar.
3. Performs, at most, the next steps operations toward completing the division algorithm.
4. Decrements steps by the number of operations consumed.
5. Returns TRUE and unlocks the matrix if the division completed.
6. Returns FALSE if the division was not attempted or steps was exhausted before the algorithm completed.

## MatrixStepRowMultiply (Method)

This method multiplies each element in toRow by scalar and stores the results back in toRow (Matrix $[t o R o w]=$ Matrix $[t o R o w] \cdot$ scalar $)$.

The operation will perform the next steps operations of the complete multiplication. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the multiplication. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise multiplication.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to multiply each entry in toRow by scalar.
3. Performs, at most, the next steps operations toward completing the multiplication algorithm.
4. Decrements steps by the number of operations consumed.
5. Returns TRUE and unlocks the matrix if the multiplication completed.
6. Returns FALSE if the multiplication was not attempted or steps was exhausted before the algorithm completed.

## MatrixStepRowSubtract (Method)

This method subtracts one row from another inside this matrix, replacing the content of the second row (Matrix[toRow] = Matrix[toRow] - Matrix[fromRow] •scalar).

The operation will perform the next steps operations of the complete subtraction. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the subtraction. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise subtraction.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to multiply fromRow by scalar and subtract the result from toRow.
3. fromRow remains unchanged.
4. Performs, at most, the next steps operations toward completing the subtraction algorithm.
5. Decrements steps by the number of operations consumed.

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6. Returns TRUE and unlocks the matrix if the subtraction completed.
7. Returns FALSE if the subtraction was not attempted or steps was exhausted before the algorithm completed.

## MatrixStepScale (Method)

Multiplies each element in this matrix by a scalar.
The operation will perform the next steps operations of the complete scaling operation. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the scaling operation. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise scaling operation.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to multiply each element in the matrix by scalar.
3. Performs, at most, the next steps operations toward completing the scaling algorithm.
4. Decrements steps by the number of operations consumed.
5. Returns TRUE and unlocks the matrix if the scaling operation completed.
6. Returns FALSE if the scaling operation was not attempted or steps was exhausted before the algorithm completed.

## MatrixTimedRowAdd (Method)

This method adds one row to another inside this matrix, replacing the content of the second row (Matrix $[$ toRow $]=$ Matrix $[$ toRow $]+$ Matrix $[$ fromRow $]$ scalar $)$.

The operation will perform work for the next duration microseconds toward completion of the addition. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the addition. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise addition.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to multiply fromRow by scalar and add the result to toRow.
3. fromRow remains unchanged.
4. Performs work toward completing the addition algorithm, in groups of steps, until duration microseconds is exceeded.
5. Decrements duration by the microseconds consumed.
6. Returns TRUE and unlocks the matrix if the addition completed.
7. Returns FALSE if the addition was not attempted or duration was exhausted before the algorithm completed.

## MatrixTimedRowDivide (Method)

This method divides each element in toRow by scalar and stores the results back in toRow (Matrix $[t o R o w]=$ Matrix[toRow] / scalar $)$.

The operation will perform work for the next duration microseconds toward the complete division. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the division. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise division.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to divide each element in toRow by scalar.
3. Performs work toward completing the division algorithm, in groups of steps, until duration microseconds is exceeded.
4. Decrements duration by the microseconds consumed.
5. Returns TRUE and unlocks the matrix if the division completed.
6. Returns FALSE if the division was not attempted or duration was exhausted before the algorithm completed.

## MatrixTimedRowMultiply (Method)

This method multiplies each element in toRow by scalar and stores the results back in toRow (Matrix $[t o R o w]=$ Matrix $[t o R o w] \cdot$ scalar $)$.

The operation will perform work for the next duration microseconds toward the complete multiplication. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the multiplication. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise multiplication.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to multiply each entry in toRow by scalar.
3. Performs work toward completing the multiplication algorithm, in groups of steps, until duration microseconds is exceeded.
4. Decrements duration by the microseconds consumed.
5. Returns TRUE and unlocks the matrix if the multiplication completed.
6. Returns FALSE if the multiplication was not attempted or duration was exhausted before the algorithm completed.

## MatrixTimedRowSubtract (Method)

This method subtracts one row from another inside this matrix, replacing the content of the second row (Matrix $[t o R o w]=$ Matrix $[t o R o w]-$ Matrix $[$ fromRow $] \cdot$ scalar $)$.

The operation will perform work for the next duration microseconds toward the complete subtraction. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion time to be a concern.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the subtraction. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise subtraction.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to multiply fromRow by scalar and subtract the result from toRow.
3. fromRow remains unchanged.
4. Performs work toward completing the subtraction algorithm, in groups of steps, until duration microseconds is exceeded.
5. Decrements duration by the microseconds consumed.
6. Returns TRUE and unlocks the matrix if the subtraction completed.
7. Returns FALSE if the subtraction was not attempted or duration was exhausted before the algorithm completed.

## MatrixTimedScale (Method)

Multiplies each element in this matrix by a scalar.
The operation will perform work for the next duration microseconds toward the complete scaling operation. This design allows for the completion of the algorithm over the course of multiple task cycles for matrices large enough for completion duration to be a concern.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method completed the scaling operation. |

## Processing

1. Validates that the matrix is initialized and has begun a stepwise scaling operation.
2. If the checks pass, this method uses the values provided in StartMatrixOperation() to multiply each element in the matrix by scalar.
3. Performs work toward completing the scaling algorithm, in groups of steps, until duration microseconds is exceeded.
4. Decrements duration by the microseconds consumed.
5. Returns TRUE and unlocks the matrix if the scaling operation completed.
6. Returns FALSE if the scaling operation was not attempted or duration was exhausted before the algorithm completed.

## RowSwap (Method)

This method exchanges the position of two rows in a given matrix.

## Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| row1 | UINT | The first row to swap. |
| row2 | UINT | The second row to swap. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method performed the row swap. |

## Processing

1. Validates that the matrix is initialized and not performing any stepwise operation.
2. If the checks pass, swaps the positions of rowl and row 2 .
3. Returns TRUE if the swap succeeded.
4. Returns FALSE if the swap failed.

## SetSize (Method)

This method changes the storage capacity of the matrix modifying Rows and Cols.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| rowCount | UINT | The new number of rows. |
| colCount | UINT | The new number of columns. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method resized the matrix. |

## Processing

1. Validates that the matrix is not performing any stepwise operation.
2. If either rowCount or colCount is zero, sets Rows and Cols to zero and frees all system resources.
3. If both rowCount equals Rows and colCount equals Cols, leaves the matrix unchanged.
4. If rowCount is greater than Rows, adds zeroed rows to the bottom of the matrix.
5. If rowCount is less than Rows, removes rows from the bottom of the matrix.
6. If colCount is greater than Cols, adds zeros to the end of each row.
7. If colCount is less than Cols, truncates each row to the new count.
8. Returns TRUE if the matrix is the newly requested size.
9. Returns FALSE if the matrix is not the newly requested size.
10. If the resize fails, the matrix retains all old values.

## StartMatrixOperation (Method)

This method must be called to configure any stepwise or timed operation on only this matrix. It accepts and stores the values used during the operation.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| operation | enum_MatrixState | The stepwise operation to begin. |
| fromRow | UINT | The row to use in the modification. Used only in addition <br> and subtraction. |
| toRow | UINT | The row to be modified. |
| scalar | struct_ComplexRect | The constant value to be used during the operation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the method locked the matrix to the requested operation. |

## Processing

1. Validates that the matrix is initialized and not performing any stepwise operation.
2. Validates row indices required for the operation requested. For addition and subtraction, both indices must be within the matrix. For multiplication and division, only toRow is validated. For scaling operations, no row index is validated
3. Stores scalar for use during the operation.
4. Locks the matrix to prevent other operations from occurring.
5. Returns TRUE if the operation is primed.
6. Returns FALSE if anything prevents the operation from being primed.

## class_MatrixAdd (Class)

This class handles the locking handshakes and the state required to add two class_Matrix objects over the course of multiple scans.

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to perform a new addition (result $=$ matrix $1+$ matrix 2 ). It must be called before each addition of two matrices to be performed.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| matrix1 | class_Matrix | The first addend. |
| matrix2 | class_Matrix | The second addend. |
| result | class_Matrix | The sum of matrix1 and matrix2. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the addition operation is now ready. |

## Processing

1. Returns FALSE if either matrixl or matrix2 is not initialized.
2. Returns FALSE if result is not a separate matrix from both matrixl and matrix2.
3. Returns FALSE if any of the three matrices is busy doing any stepwise operation.
4. Returns FALSE if the dimensions of matrixl do not match those of matrix2.
5. Returns FALSE if result cannot be made to be the same dimensions as the other two matrices.
6. Returns FALSE if it cannot lock all matrices involved in the operation.
7. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.
8. The contents of result are destroyed by this method.

## ProcessSteps (Method)

This method performs the addition algorithm on three already locked-in matrices.
The operation will perform the next steps sub-operations of the complete addition algorithm.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the addition completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Adds each element in matrixl to its corresponding element in matrix 2 and stores the sum in result.
3. Decrements steps by the number of operations performed.
4. Returns TRUE if the addition algorithm completed before steps was exhausted.
5. Returns FALSE if LockMatrices() has not been called or steps was exhausted before completing the algorithm.

## ProcessTimed (Method)

This method performs the addition algorithm on three already locked-in matrices.
The operation will perform work for the next duration microseconds toward the complete addition algorithm.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the addition completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Adds each element in matrixl to its corresponding element in matrix2 and stores the sum in result.
3. Performs work toward completing the addition algorithm, in groups of steps, until duration microseconds is exceeded.
4. Decrements duration by the microseconds consumed.
5. Returns TRUE if the addition algorithm completed before duration was exhausted.
6. Returns FALSE if LockMatrices() has not been called or duration was exhausted before completing the algorithm.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices (). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## class_MatrixCopyColumn (Class)

This class handles the locking handshakes and the state required to copy a column from one class_Matrix object to another over the course of multiple scans.

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to perform a new column copy. It must be called before each column copy to be performed.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| fromColumn | UINT | The index of the column to copy from. |
| toColumn | UINT | The index of the column to copy to. |

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| fromMatrix | class_Matrix | The matrix to be copied from. |
| toMatrix | class_Matrix | The matrix to be copied to. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the copy operation is now ready. |

## Processing

1. Returns FALSE if either fromMatrix or toMatrix is not initialized.
2. Returns FALSE if either of the matrices is busy doing any stepwise operation.
3. Returns FALSE if Rows of matrixl does not match Rows of matrix2.
4. Returns FALSE if either index provided is outside of the corresponding matrix.
5. Returns FALSE if it cannot lock all matrices involved in the operation.
6. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.

## ProcessSteps (Method)

This method performs the copy algorithm on two already locked-in matrices.
The operation will perform the next steps sub-operations of the complete copy.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the copy completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Copies each element in column fromColumn of fromMatrix to its corresponding element in column toColumn of toMatrix.
3. Decrements steps by the number of sub-operations performed.
4. Returns TRUE if the copy algorithm completed before steps was exhausted.
5. Returns FALSE if LockMatrices () has not been called or steps was exhausted before completing the algorithm.

## ProcessTimed (Method)

This method performs the copy algorithm on two already locked-in matrices.
The operation will perform work for the next duration microseconds toward the complete copy.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the copy completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Copies each element in column fromColumn of fromMatrix to its corresponding element in column toColumn of toMatrix.
3. Performs work toward completing the copy algorithm, in groups of steps, until duration microseconds is exceeded.
4. Decrements duration by the microseconds consumed.
5. Returns TRUE if the copy algorithm completed before duration was exhausted.
6. Returns FALSE if LockMatrices () has not been called or duration was exhausted before completing the algorithm.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices(). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## class_MatrixDeterminant (Class)

This class handles the locking handshakes and the state required to calculate the determinant of a matrix over the course of multiple scans.

If the purpose behind calculating the determinant is a check before inverting a matrix or as part of the process of solving a system of equations this class is not the most optimal to use. In these cases it is better to use the class_MatrixInvert or the class_MatrixGaussianElim object instead as the overhead for all three is similar.

Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to calculate the determinant of a new matrix. It must be called before each operation to be performed.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| original | class_Matrix | The matrix to calculate the determinant of. This matrix is <br> left unchanged. |
| workspace | class_Matrix | Memory to do the calculation in. If this is the same size <br> as original, no memory allocation will occur in finding the <br> determinant. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the operation is now ready. |

## Processing

1. Returns FALSE if original is not initialized.
2. Returns FALSE if workspace is not a separate matrix from original.
3. Returns FALSE if either of the matrices is busy doing any stepwise operation.
4. Returns FALSE if original is not a square matrix.

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5. Returns FALSE if workspace cannot be resized to the correct dimensions.
6. Returns FALSE if it cannot lock all matrices involved in the operation.
7. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.
8. The contents of workspace are destroyed by this method.

## ProcessSteps (Method)

This method computes the determinant of an already locked-in matrix.
The operation will perform the next steps sub-operations of the complete task.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| determinant | struct_ComplexRect | The determinant of the matrix. Zero if the calculation is <br> incomplete or the matrix is not invertible. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the operation completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Decrements steps by the number of sub-operations performed.
3. Returns TRUE and outputs the calculated determinant if the algorithm completed before steps was exhausted.
4. Returns FALSE and outputs a determinant of zero if LockMatrices() has not been called or steps was exhausted before completing the algorithm.
5. In the case that the matrix is not invertible, outputs a determinant of zero.

## ProcessTimed (Method)

This method computes the determinant of an already locked-in matrix.
The operation will perform work for the next duration microseconds toward the complete matrix operation.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| determinant | struct_ComplexRect | The determinant of the matrix. Zero if the calculation is <br> incomplete or the matrix is not invertible. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the operation completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Performs work toward completing the algorithm, in groups of steps, until duration microseconds is exceeded.
3. Decrements duration by the microseconds consumed.
4. Returns TRUE and outputs the calculated determinant if the operation completed before duration was exhausted.
5. Returns FALSE and outputs a determinant of zero if LockMatrices() has not been called or duration was exhausted before completing the algorithm.
6. In the case that the matrix is not invertible, outputs a determinant of zero.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices(). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## class_MatrixGaussianElim (Class)

This class handles the locking handshakes and the state required to simplify the matrix to a diagonal ones matrix with trailing columns using Gaussian elimination over the course of multiple scans. The contents of coefficients are destroyed and the contents of solutions are modified by this class.

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to perform the Gaussian elimination. It must be called before each calculation to be performed.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| coefficients <br> solutions | class_Matrix <br> class_Matrix | The coefficients of the variables being solved for. <br> The right hand side of the system of equations. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the Gaussian elimination is now ready. |

## Processing

1. Returns FALSE if either matrix is not initialized.
2. Returns FALSE if coefficients is not a separate matrix from solutions.
3. Returns FALSE if either matrix is busy doing any stepwise operation.
4. Returns FALSE if coefficients has fewer columns than rows.
5. Returns FALSE if solutions is not one column with the same number of rows as coefficients.
6. Returns FALSE if it cannot lock both matrices involved in the operation.
7. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.

## ProcessSteps (Method)

This method performs Gaussian elimination on two already locked-in matrices.

The operation will perform the next steps sub-operations of the complete calculation.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| error | BOOL | This algorithm cannot solve this system of equations. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the Gaussian elimination completed. |

## Processing

1. Validates that LockMatrices () has been successfully called.
2. Reduces the first Rows • Rows of coefficients to an identity matrix using elementary row operations.
3. Performs the same row operations on solutions.
4. If at any time the row operations cannot reduce coefficients further and there is still not an identity matrix on the left, the operation is terminated and error is set.
5. Decrements steps by the number of operations performed.
6. Returns TRUE if the Gaussian elimination completed before steps was exhausted.
7. Returns FALSE if LockMatrices() has not been called or steps was exhausted before completing the algorithm.
8. The contents of coefficients are destroyed and the contents of solutions are modified by this method.

## Output Combination Meanings

| Error | Return | Description |
| :--- | :--- | :--- |
| FALSE | FALSE | This should never occur. |
| FALSE | TRUE | The Gaussian elimination completed successfully. |
| TRUE | FALSE | The matrix state prevented the Gaussian elimination request. |
| TRUE | TRUE | The matrix is not invertible and cannot be reduced by this Gaussian elimi- <br> nation algorithm. |

## ProcessTimed (Method)

This method performs Gaussian elimination on two already locked-in matrices.
The operation will perform work for the next duration microseconds toward the complete inversion algorithm.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| error | BOOL | This algorithm cannot solve this system of equations. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the Gaussian elimination completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Reduces the first Rows • Rows of coefficients to an identity matrix using elementary row operations.
3. Performs the same row operations on solutions.
4. If at any time the row operations cannot reduce coefficients further and there is still not an identity matrix on the left, the operation is terminated and error is set.
5. Performs work toward completing the algorithm, in groups of steps, until duration microseconds is exceeded.
6. Decrements duration by the microseconds consumed.
7. Returns TRUE if the Gaussian elimination completed before duration was exhausted.
8. Returns FALSE if LockMatrices () has not been called or duration was exhausted before completing the algorithm.
9. The contents of coefficients are destroyed and the contents of solutions are modified by this method.

The table, listed for the previous method, is provided as reference for interpreting output combinations.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices (). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## class_MatrixInvert (Class)

This class handles the locking handshakes and the state required to create the inverse of a square matrix over the course of multiple scans. The contents of original are destroyed in the process so if the data are still desired, they must be copied before this class is used. The entire operation will complete before the function returns.

One common use case for inverting a matrix is to solve a system of equations. In this library that use case is discouraged unless solving the same system for many solutions as Gaussian elimination performs the same functionality with less overhead.

Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to invert a matrix. (result $=$ original $^{-1}$ ). It must be called before each inversion to be performed.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| original | class_Matrix | The matrix to invert. |
| result | class_Matrix | The inverted matrix. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the inversion operation is now ready. |

## Processing

1. Returns FALSE if original is not initialized.
2. Returns FALSE if result is not a separate matrix from original.
3. Returns FALSE if any of the matrices is busy doing any stepwise operation.
4. Returns FALSE if original is not a square matrix.
5. Returns FALSE if result cannot be sized correctly to store the product.
6. Returns FALSE if it cannot lock all matrices involved in the operation.
7. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.
8. The contents of result are destroyed by this method.

## ProcessSteps (Method)

This method performs the inversion algorithm on two already locked-in matrices.
The operation will perform the next steps sub-operations of the complete inversion algorithm.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| error | BOOL | The matrix is not invertible. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the inversion completed. |

## Processing

1. Validates that LockMatrices () has been successfully called.
2. Sets result to an identity matrix.
3. Reduces original to an identity matrix using elementary row operations.
4. Performs the same row operations on result to create the inverse.
5. If at any time the row operations cannot reduce original further and it is still not an identity matrix, the operation is terminated and error is set.
6. Decrements steps by the number of operations performed.
7. Returns TRUE if the inversion algorithm completed before steps was exhausted.
8. Returns FALSE if LockMatrices () has not been called or steps was exhausted before completing the algorithm.
9. The contents of original are destroyed by this method.

## ProcessTimed (Method)

This method performs the inversion algorithm on two already locked-in matrices.
The operation will perform work for the next duration microseconds toward the complete inversion algorithm.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| error | BOOL | The matrix is not invertible. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the inversion completed. |

## Processing

1. Validates that LockMatrices () has been successfully called.
2. Sets result to an identity matrix.
3. Reduces original to an identity matrix using elementary row operations.
4. Performs the same row operations on result to create the inverse.
5. If at any time the row operations cannot reduce original further and it is still not an identity matrix, the operation is terminated and error is set.
6. Performs work toward completing the algorithm, in groups of steps, until duration microseconds is exceeded.
7. Decrements duration by the microseconds consumed.
8. Returns TRUE if the inversion algorithm completed before duration was exhausted.
9. Returns FALSE if LockMatrices () has not been called or duration was exhausted before completing the algorithm.
10. The contents of original are destroyed by this method.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices (). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## class_MatrixMultiply (Class)

This class handles the locking handshakes and the state required to multiply two class_Matrix objects over the course of multiple scans.

Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to perform a new multiply (result = matrix $1 \cdot$ matrix 2 ). It must be called before each multiply to be performed.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| matrix1 | class_Matrix | The multiplicand. |
| matrix2 | class_Matrix | The multiplier. |
| result | class_Matrix | The matrix to store the product. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the multiply operation is now ready. |

## Processing

1. Returns FALSE if either matrixl or matrix2 is not initialized.
2. Returns FALSE if result is not a separate matrix from both matrixl and matrix2.
3. Returns FALSE if any of the matrices are busy doing any stepwise operation.
4. Returns FALSE if Cols of matrixl does not match Rows of matrix2.
5. Returns FALSE if result cannot be sized correctly to store the product.
6. Returns FALSE if it cannot lock all matrices involved in the operation.
7. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.
8. The contents of result are destroyed by this method.

## ProcessSteps (Method)

This method performs the multiplication algorithm on three already locked-in matrices.
The operation will perform the next steps sub-operations of the complete multiplication algorithm.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the multiplication completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Multiplies matrixl by matrix2.
3. Decrements steps by the number of operations performed.
4. Returns TRUE if the multiply algorithm completed before steps was exhausted.
5. Returns FALSE if LockMatrices () has not been called or steps was exhausted before completing the algorithm.

## ProcessTimed (Method)

This method performs the multiplication algorithm on three already locked-in matrices.
The operation will perform work for the next duration microseconds toward the complete multiplication algorithm.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the multiplication completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Multiplies matrixl by matrix2.
3. Performs work toward completing the multiplication algorithm, in groups of steps, until duration microseconds is exceeded.
4. Decrements duration by the microseconds consumed.
5. Returns TRUE if the multiply algorithm completed before duration was exhausted.
6. Returns FALSE if LockMatrices () has not been called or duration was exhausted before completing the algorithm.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices (). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## class_MatrixSubtract (Class)

This class handles the locking handshakes and the state required to subtract one class_Matrix object from another over the course of multiple scans.

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to perform a new subtraction (result = matrix1 - matrix2). It must be called before each subtraction to be performed.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| matrix1 | class_Matrix | The minuend. |
| matrix2 | class_Matrix | The subtrahend. |
| result | class_Matrix | The difference of matrix1 - matrix2. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the subtraction operation is now ready. |

## Processing

1. Returns FALSE if either matrixl or matrix2 is not initialized.
2. Returns FALSE if result is not a separate matrix from both matrixl and matrix2.
3. Returns FALSE any of the matrices are busy doing any stepwise operation.
4. Returns FALSE if the dimensions of matrixl do not match those of matrix2.
5. Returns FALSE if result cannot be resized to match the dimensions of the other two matrices.
6. Returns FALSE if it cannot lock all matrices involved in the operation.
7. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.
8. The contents of result are destroyed by this method.

## ProcessSteps (Method)

This method performs the subtraction algorithm on three already locked-in matrices.
The operation will perform the next steps sub-operations of the complete subtraction algorithm.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the subtraction completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Subtracts each element in matrix 2 from its corresponding element in matrixl and the difference in result.
3. Decrements steps by the number of sub-operations performed.
4. Returns TRUE if the subtraction algorithm completed before steps was exhausted.
5. Returns FALSE if LockMatrices() has not been called or steps was exhausted before completing the algorithm.

## ProcessTimed (Method)

This method performs the subtraction algorithm on three already locked-in matrices.
The operation will perform work for the next duration microseconds toward the complete subtraction algorithm.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the subtraction completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Subtracts each element in matrix 2 from its corresponding element in matrixl and stores the difference in result.
3. Performs work toward completing the subtraction algorithm, in groups of steps, until duration microseconds is exceeded.
4. Decrements duration by the microseconds consumed.
5. Returns TRUE if the subtraction algorithm completed before duration was exhausted.
6. Returns FALSE if LockMatrices () has not been called or duration was exhausted before completing the algorithm.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices(). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## class_MatrixTranspose (Class)

This class handles the locking handshakes and the state required to transpose a class_Matrix object over the course of multiple scans.

Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to perform a new matrix transpose. It must be called before each transpose to be performed.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| conjugate | BOOL | The result of this operation will be the Hermitian Transpose. <br> Before each element is placed in result, it will be conjugated. |

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| original | class_Matrix | The matrix to copy from. |
| result | class_Matrix | The matrix to copy to. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the transpose operation is now ready. |

## Processing

1. Returns FALSE if original is not initialized.
2. Returns FALSE if result is not a separate matrix from original.
3. Returns FALSE if either of the matrices is busy doing any stepwise operation.
4. Returns FALSE if result cannot be resized to the correct dimensions.
5. Returns FALSE if it cannot lock all matrices involved in the operation.
6. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.
7. The contents of result are destroyed by this method.

## ProcessSteps (Method)

This method transposes an already locked-in matrix.
The operation will perform the next steps sub-operations of the complete matrix transpose.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the transpose completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Copies each element $(\mathrm{i}, \mathrm{j})$ from original to element $(\mathrm{j}, \mathrm{i})$ of result.
3. If conjugate was TRUE, conjugate each element in result.
4. Decrements steps by the number of sub-operations performed.
5. Returns TRUE if the transpose algorithm completed before steps was exhausted.
6. Returns FALSE if LockMatrices() has not been called or steps was exhausted before completing the algorithm.

## ProcessTimed (Method)

This method transposes an already locked-in matrix.
The operation will perform work for the next duration microseconds toward the complete matrix transpose.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the transpose completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Copies each element $(\mathrm{i}, \mathrm{j})$ from original to element $(\mathrm{j}, \mathrm{i})$ of result.
3. If conjugate was TRUE, conjugate each element in result.
4. Performs work toward completing the transpose, in groups of steps, until duration microseconds is exceeded.
5. Decrements duration by the microseconds consumed.
6. Returns TRUE if the transpose algorithm completed before duration was exhausted.
7. Returns FALSE if LockMatrices() has not been called or duration was exhausted before completing the algorithm.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices(). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## class_Matrix_ATA (Class)

This class handles the locking handshakes and the state required for an optimization of the operation $\left(A^{T} A\right)$ transposing the input matrix and multiplying it by the original matrix over the course of multiple scans.

## Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| Busy | BOOL | This class has locked class_Matrix instances and is in the middle <br> of a calculation. |

## LockMatrices (Method)

This method primes the class to perform a new matrix operation $A^{T} A$. It must be called before each operation to be performed.

Inputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| conjugate | BOOL | The result of this operation will be calculated using the Her- <br> mitian Transpose. Before the transpose step is complete, each <br> element will be conjugated. |

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| original | class_Matrix | The matrix A. |
| result | class_Matrix | The matrix for the result. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the operation is now ready. |

## Processing

1. Returns FALSE if original is not initialized.
2. Returns FALSE if result is not a separate matrix from original.
3. Returns FALSE if either of the matrices is busy doing any stepwise operation.
4. Returns FALSE if result cannot be resized to the correct dimensions.
5. Returns FALSE if it cannot lock all matrices involved in the operation.
6. If all other checks succeeded, then stores required references, sets Busy to TRUE, and returns TRUE.
7. The contents of result are destroyed by this method.

## ProcessSteps (Method)

This method computes $\mathrm{A}^{\mathrm{T}} \mathrm{A}$ of an already locked-in matrix.
The operation will perform the next steps sub-operations of the complete task.

## Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| steps | UDINT | The number of sub-operations to attempt this task cycle. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the operation completed. |

## Processing

1. Validates that LockMatrices() has been successfully called.
2. Decrements steps by the number of sub-operations performed.
3. Returns TRUE if the algorithm completed before steps was exhausted.
4. Returns FALSE if LockMatrices () has not been called or steps was exhausted before completing the algorithm.

## ProcessTimed (Method)

This method computes $\mathrm{A}^{\mathrm{T}} \mathrm{A}$ of an already locked-in matrix.
The operation will perform work for the next duration microseconds toward the complete matrix operation.

Inputs/Outputs

| Name | IEC 61131 Type | Description |
| :--- | :--- | :--- |
| duration | UDINT | The number of microseconds to spend on this calculation. |

## Return Value

| IEC 61131 Type | Description |
| :--- | :--- |
| BOOL | Returns TRUE if the operation completed. |

## Processing

1. Validates that LockMatrices () has been successfully called.
2. Performs work toward completing the algorithm, in groups of steps, until duration microseconds is exceeded.
3. Decrements duration by the microseconds consumed.
4. Returns TRUE if the operation completed before duration was exhausted.
5. Returns FALSE if LockMatrices() has not been called or duration was exhausted before completing the algorithm.

## UnlockMatrices (Method)

This method unlocks any matrices locked by LockMatrices (). It only needs to be called by the user if the matrix operation has been terminated early by calling Clear () on any of the dependent matrices. In all other cases, the matrices will be unlocked on completion of the algorithm.

## Processing

1. Requests that all locked matrices free themselves for other operations.
2. Sets Busy to FALSE.

## Benchmarks

## Benchmark Platforms

The benchmarking tests recorded for this library are performed on the following platforms.
SEL-3505
$>$ R134 firmware
SEL-3530
$>$ R134 firmware
SEL-3555
$>$ Dual-core Intel i7-3555LE processor
$>4$ GB ECC RAM
$>$ R134-V1 firmware

## Benchmark Test Descriptions

Each benchmark is run on three different matrices: a 2 by 2 , an 8 by 8 , and a 64 by 64 . All matrices used in the benchmarks are sized such that no memory allocations occur during the benchmark run.

## fun_DeleteMatrix

The posted time is the average execution time of 100 consecutive calls when deleting a matrix.

## fun_MatrixAdd

The posted time is the average execution time of 100 consecutive calls when adding two matrices.

## fun_MatrixCopyColumn

The posted time is the average execution time of 100 consecutive calls when copying a column from one matrix to another.

## fun_MatrixDeterminant

The posted time is the average execution time of 100 consecutive calls when operating on a valid invertable matrix.

## fun_MatrixGaussianElim

The posted time is the average execution time of 100 consecutive calls when operating on a valid matrix that allows the algorithm to run to completion.

## fun_MatrixInvert

The posted time is the average execution time of 100 consecutive calls when inverting a matrix.

## fun_MatrixMultiply

The posted time is the average execution time of 100 consecutive calls when multiplying two matrices.

## fun_MatrixSubtract

The posted time is the average execution time of 100 consecutive calls when subtracting two matrices.

## fun_MatrixTranspose

The posted time is the average execution time of 100 consecutive calls when transposing a matrix.

## fun_MatrixTranspose (Hermitian)

The posted time is the average execution time of 100 consecutive calls when calculating the Hermitian transpose of a matrix.

## fun_Matrix_ATA

The posted time is the average execution time of 100 consecutive calls when calculating $\mathrm{A}^{\mathrm{T}} \mathrm{A}$.

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## fun_Matrix_ATA (Hermitian)

The posted time is the average execution time of 100 consecutive calls when calculating $\mathrm{A}^{\mathrm{T}} \mathrm{A}$ when using the Hermitian transpose.

## fun_NewMatrix

The posted time is the average execution time of 100 consecutive calls when allocating a new matrix.

## Benchmark Results

| Operation Tested | Platform (time in $\mu s$ ) |  |  |
| :---: | :---: | :---: | :---: |
|  | SEL-3505 | SEL-3530 | SEL-3555 |
| fun_DeleteMatrix - 2 x 2 | 118 | 54 | 6 |
| fun_DeleteMatrix - 8x8 | 105 | 49 | 4 |
| fun_DeleteMatrix - 64x64 | 119 | 57 | 4 |
| fun_MatrixAdd - $2 \times 2$ | 17 | 7 | 1 |
| fun_MatrixAdd - 8x8 | 66 | 46 | 4 |
| fun_MatrixAdd - $64 \times 64$ | 5408 | 3299 | 244 |
| fun_MatrixCopyColumn - $2 \times 2$ | 7 | 2 | 1 |
| fun_MatrixCopyColumn - 8x8 | 10 | 3 | 1 |
| fun_MatrixCopyColumn - 64x64 | 61 | 36 | 1 |
| fun_MatrixDeterminant - $2 \times 2$ | 69 | 41 | 3 |
| fun_MatrixDeterminant - 8x8 | 1118 | 665 | 53 |
| fun_MatrixDeterminant - 64x64 | 515458 | 292846 | 26267 |
| fun_MatrixGaussianElim - $2 \times 2$ | 76 | 39 | 2 |
| fun_MatrixGaussianElim - 8x8 | 1392 | 731 | 61 |
| fun_MatrixGaussianElim - 64x64 | 516370 | 296721 | 26789 |
| fun_MatrixInvert - $2 \times 2$ | 74 | 48 | 3 |
| fun_MatrixInvert - 8x8 | 2092 | 1243 | 105 |
| fun_MatrixInvert - 64x64 | 1034455 | 581496 | 52648 |
| fun_MatrixMultiply - $2 \times 2$ | 26 | 15 | 2 |
| fun_MatrixMultiply - 8x8 | 1002 | 626 | 51 |
| fun_MatrixMultiply - $64 \times 64$ | 554947 | 325479 | 26534 |
| fun_MatrixSubtract - $2 \times 2$ | 13 | 6 | 1 |
| fun_MatrixSubtract - 8x8 | 90 | 41 | 4 |
| fun_MatrixSubtract - $64 \times 64$ | 5341 | 3066 | 242 |
| fun_MatrixTranspose - $2 \times 2$ | 8 | 4 | 1 |
| fun_MatrixTranspose - 8x8 | 29 | 12 | 1 |
| fun_MatrixTranspose - 64x64 | 2447 | 1731 | 71 |
| fun_MatrixTranspose (Hermitian) - $2 \times 2$ | 14 | 7 | 1 |
| fun_MatrixTranspose (Hermitian) - 8x8 | 97 | 48 | 3 |
| fun_MatrixTranspose (Hermitian) - 64x64 | 6071 | 3699 | 192 |
| fun_Matrix_ATA - $2 \times 2$ | 26 | 15 | 1 |
| fun_Matrix_ATA - 8x8 | 563 | 318 | 29 |
| fun_Matrix_ATA - $64 \times 64$ | 308482 | 179945 | 13186 |
| fun_Matrix_ATA (Hermitian) - 2x2 | 34 | 19 | 1 |


| Operation Tested | Platform (time in $\mu s$ ) |  |  |
| :--- | ---: | ---: | ---: |
|  | SEL-3505 | SEL-3530 | SEL-3555 |
| fun_Matrix_ATA (Hermitian) $-8 \times 8$ | 877 | 455 | 39 |
| fun_Matrix_ATA (Hermitian) $-64 \times 64$ | 431940 | 239407 | 17341 |
| fun_NewMatrix $-2 \times 2$ | 340 | 98 | 10 |
| fun_NewMatrix $-8 \times 8$ | 87 | 39 | 5 |
| fun_NewMatrix $-64 \times 64$ | 744 | 327 | 13 |

## Examples

These examples demonstrate the capabilities of this library. Do not mistake them as suggestions or recommendations from SEL.

Implement the best practices of your organization when using these libraries. As the user of this library, you are responsible for ensuring correct implementation and verifying that the project using these libraries performs as expected.

## Solving a System of Equations

## Objective

The user desires to repeatably solve a system of equations for some set of outputs. This example solves three equations for three unknowns.

For example, on a given scan the system of equations could be:

$$
\left\{\begin{array}{l}
x+2 y+3 z=2 \\
2 x+3 y+z=2 \\
3 x+2 y+z=10
\end{array}\right.
$$

This becomes a $3 \times 4$ matrix which, after Gaussian elimination, appears as follows:

$$
\left[\begin{array}{ccc|c}
1 & 2 & 3 & 2 \\
2 & 3 & 1 & 2 \\
3 & 2 & 1 & 10
\end{array}\right]=>\left[\begin{array}{lll|c}
1 & 0 & 0 & 5 \\
0 & 1 & 0 & -3 \\
0 & 0 & 1 & 1
\end{array}\right]
$$

By inspection the solution becomes:

$$
\left\{\begin{array}{l}
x=5 \\
y=-3 \\
z=1
\end{array}\right.
$$

## Assumptions

Each scan the user has placed the values to use into a pair of arrays of struct_ComplexRect objects, Values and Answers, before this program is called.

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Examples

## Solution

The user can call this program each scan to receive a solution for the provided inputs, as shown in Code Snippet 1.

## Code Snippet 1 prg_MatrixSolver

```
PROGRAM prg_MatrixSolver
VAR
    (* Here are sample values to generate a matrix with a known solution
        [[[lllllll
        [lllllll
        [\begin{array}{llllll}{3}&{2}&{1}&{|}&{10}\end{array}]
    Values : ARRAY [0 .. 8] OF struct_ComplexRect :=
        [(Re := 1), (Re := 2), (Re := 3),
            (Re := 2), (Re := 3), (Re := 1),
            (Re := 3), (Re := 2), (Re := 1)];
    AnswerCol : ARRAY [0 . 2] OF struct_ComplexRect :=
        [(Re := 2), (Re := 2), (Re := 10)];
    // The result should be [5, -3, 1]
    Solution : ARRAY [0 .. 2] OF struct_ComplexRect;
    CoefficientsMatrix : class_Matrix(3, 3);
    SolutionsMatrix : class_Matrix(3, 1);
    pt_Data : POINTER TO POINTER TO struct_ComplexRect;
    Unsolved : BOOL;
    Row : UINT;
    Col : UINT;
END_VAR
```

//Load each row of the matrix
FOR Row := 0 to CoefficientsMatrix.Rows - 1 DO
pt_Data := CoefficientsMatrix.pt_Data;
//Load all but the answer column of the matrix
FOR Col := 0 TO CoefficientsMatrix.Cols - 1 DO
pt_Data[Row][Col] := Values[Row*(CoefficientsMatrix.Cols) + Col];
END_FOR
//Load the answer column after the final increment above
pt_Data := SolutionsMatrix.pt_Data;
pt_Data[Row] [0] := AnswerCol[Row];
END_FOR
fun_MatrixGaussianElim(CoefficientsMatrix, SolutionsMatrix, error =>
Unsolved);
FOR Row := 0 to SolutionsMatrix.Rows - 1 DO
//If a solution was successfully found update the solution array.
IF NOT Unsolved THEN
pt_Data := SolutionsMatrix.pt_Data;
Solution[Row] := pt_Data[Row] [0];
END_IF
END_FOR

## Manipulating a Matrix Across Multiple Scans

## Objective

The user needs to manipulate a set of data in matrix form, but has some set of timing constraints that cause concern regarding the completion of the operations.

## Assumptions

The user has created an enumeration to assist in managing the data flow to the desired outcome.

Code Snippet 2 enum_States

```
TYPE enum_States :
(
    IDLE,
    BUILD_MATRICES,
    SUM_MATRICES,
    SCALE_RESULT,
    STORE_RESULT,
    ERROR
);
END_TYPE
```


## Solution

The user can call this program each scan, as shown in Code Snippet 3, to receive a solution for the provided inputs. When Begin is set to true, the calculation will commence. When the program has copied the answer into Solution, the program sets the Complete flag to true.

Code Snippet 3 prg_MatrixManipulation

```
PROGRAM prg_MatrixManipulation
VAR CONSTANT
    c_StepsPerScan : UDINT := 5;
END_VAR
VAR
    State : enum_States := IDLE;
    Values1 : ARRAY [0 .. 11] OF struct_ComplexRect;
    Values2 : ARRAY [0 . . 11] OF struct_ComplexRect;
    Solution : ARRAY [0 .. 11] OF struct_ComplexRect;
    Matrix1 : class_Matrix(4, 3);
    Matrix2 : class_Matrix(4, 3);
    MatrixEnd : class_Matrix(4, 3);
    Adder : class_MatrixAdd;
    Scalar : struct_ComplexRect := (Re := 2, Im := 0);
    pt_Data1 : POINTER TO POINTER TO struct_ComplexRect;
    pt_Data2 : POINTER TO POINTER TO struct_ComplexRect;
    Row : UINT;
    Col : UINT;
    Steps : UDINT;
    Scans : UDINT;
    Begin : BOOL;
    Complete : BOOL;
END_VAR
```


## Code Snippet 3 prg_MatrixManipulation (Continued)

```
Steps := c_StepsPerScan;
Scans := Scans + 1;
WHILE Steps > O DO
    CASE State OF
    IDLE:
        IF Begin THEN
            State := BUILD_MATRICES;
            Row := 0;
            Col := 0;
            Scans := 1;
            pt_Data1 := Matrix1.pt_Data;
            pt_Data2 := Matrix2.pt_Data;
            Begin := FALSE;
            Complete := FALSE;
            Steps := Steps - 1;
        ELSE
            Scans := Scans - 1;
            Steps := 0;
        END_IF
    BUILD_MATRICES:
                //This is a state machine to load the matrix a few values at a time
        Steps := Steps - 1;
        pt_Data1[Row][Col] := Values1[Row*(Matrix1.Cols) + Col];
        pt_Data2[Row] [Col] := Values2[Row*(Matrix1.Cols) + Col];
        Col := Col + 1;
        IF Col = Matrix1.Cols THEN
            Col := 0;
            Row := Row + 1;
            IF Row = Matrix1.Rows THEN
                IF Adder.LockMatrices(Matrix1, Matrix2, MatrixEnd) THEN
                    State := SUM_MATRICES;
                    ELSE
                            State := ERROR;
                END_IF
            END_IF
        END_IF
    SUM_MATRICES:
        IF Adder.ProcessSteps(steps) THEN
            IF MatrixEnd.StartMatrixOperation(MATRIX_SCALE, 0, 0, Scalar)
                    THEN
                State := SCALE_RESULT;
            ELSE
                State := ERROR;
            END_IF
        END_IF
    SCALE_RESULT:
        IF MatrixEnd.MatrixStepScale(steps) THEN
            State := STORE_RESULT;
            Row := 0;
            Col := 0;
        END_IF
```

Code Snippet 3 prg_MatrixManipulation (Continued)

```
    STORE_RESULT:
```

        Steps := Steps - 1;
        Solution[Row*(MatrixEnd.Cols) + Col] := MatrixEnd.pt_Data[Row] [Col];
        Col := Col +1 ;
        IF Col = MatrixEnd.Cols THEN
            Col := 0;
            Row := Row + 1 ;
            IF Row = MatrixEnd.Rows THEN
                State := IDLE;
                Complete := TRUE;
                Steps := 0;
            END_IF
        END_IF
    ERROR:
        Steps := 0;
    END_CASE
    END_WHILE

## Troubleshooting a Matrix

## Objective

The user has designed a solution with matrices to perform some set of calculations and something is not going as desired. The user would like to have additional insight into the matrix element values for online troubleshooting.

## Assumptions

This solution assumes a static matrix size. This is not required but if the Rows and Cols variables of the matrix do not match the sizes provided for the troubleshooting variable, the user must realize that only data up to the size of the matrix are valid.

## Solution

The user can add an additional pointer variable to provide additional insight during runtime. The syntax for this pointer is shown in Code Snippet 4.

## Code Snippet 4 prg_MatrixTroubleshoot

```
PROGRAM prg_MatrixTroubleshoot
VAR CONSTANT
    c_Rows : UINT := 2;
    c_Cols : UINT := 6;
END_VAR
VAR
    Values1 : ARRAY [0 .. 11] OF struct_ComplexRect;
    Matrix1 : class_Matrix(c_Rows, c_Cols);
    **This is the troubleshooting variable that has been added.
        To be valid it must be reassigned each time the memory allocated to
        the matrix could change, so the safest usage is to assign it
            immediately
        before using it.*)
    pt_Raw : POINTER TO ARRAY [0 .. c_Rows-1] OF
            POINTER TO ARRAY [0 .. c_Cols-1] OF struct_ComplexRect;
```

END_VAR

```
//Load the matrix
(*The SysMemCpy command allows the movement of large quantities of
    contiguous
    data with a single instruction. This can greatly increase the performance
    of large data copies. If the destination and the source could overlap
    then the SysMemMove call facilitates this with a little more overhead.*)
SysMemCpy(Matrix1.pt_Data[0], ADR(Values1),
    c_Cols*SIZEOF(struct_ComplexRect));
SysMemCpy(Matrix1.pt_Data[1], ADR(Values1[6]),
    c_Cols*SIZEOF(struct_ComplexRect));
(*Here is where we find some meaningful work up to the point of interest
    for troubleshooting.*)
//Assign the troubleshooting variable. Now the data can be seen in
//online mode.
//This line is where a breakpoint would be added.
pt_Raw := Matrix1.pt_Data;
(*There is probably additional work to be accomplished after the point of
    interest as well*)
```


## Release Notes

| Version | Summary of Revisions | Date Code |
| :---: | :--- | :---: |
| 3.5.1.1 | $>$ Allows new versions of ACSELERATOR RTAC to compile projects <br> for previous firmware versions without SEL IEC types "Cannot <br> convert" messages. | 20180921 |
| $>$ Must be used with R143 firmware or later. |  |  |

